

Ion Transport and Limited Currents in Supporting Electrolytes and Ionic Liquids

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Abstract:

Supporting electrolytes contain inert dissolved salts to increase the conductivity, to change microenvironments near the electrodes and to assist in electrochemical reactions. Herein, a combined experimental and computational study examines the impact of supporting salts on the ion transport and limited currents of electrochemical reactions. A physical model that describes multi-ion transport in liquid electrolytes and the related concentration gradients is discussed. This model and its parameterization are evaluated by the measured limited current of the copper deposition in a CuSO_4 electrolyte under a gradually increasing amount of Na_2SO_4 that acts as a supporting salt. A computational sensibility analysis of the transport model reveals that the shared conductance between the ions lowers the limited currents with larger supporting salt concentrations. When the supporting salt supplies most of the conductance, the electric-field-driven transport of the electrochemically active ions becomes negligible so that the limited current drops to the diffusion-limited current that is described by Fick's first law. The transition from diluted supporting electrolyte to the case of ionic liquids is elucidated with the transport model, highlighting the different physical transport mechanisms in a non-conducting (polar) and a conducting (ionic) solvent.

1 Introduction

Supporting electrolytes are solvent-based liquids that contain inert salt additives (defined as supporting salts) which are not electrochemically converted. These additive salts can increase the conductivity of the electrolyte and thereby improve the efficiency of electrochemical processes^{1–3}. For example, in industrial copper refining and winning the conductivity of aqueous CuSO_4 baths is increased by H_2SO_4 addition^{4,5}. Supported electrolytes with at least three different sorts of ions also emerge when reactive ion types are dissolved in for instance aqueous solutions^{6–8}, molten salts^{9–11}, deep eutectic solvents^{12,13}, or ionic liquids^{14–17}.

For binary (one type of cation and one type of anion) solvent-based electrolytes the transport of ions was experimentally characterized and theoretically described in various works^{18–20}. In these systems, the electrolyte is thinning out at the electrode at which dissolved ions are electrochemically converted, whereas the ions accumulate at the electrode which introduces them into the electrolyte. Thus, electrochemical reactions cause concentration gradients in liquid electrolytes^{21–23} that ultimately limit the current that electric-field and diffusion-driven ion transport can carry without locally depleting the concentration of the converted ion types²⁴. The limited currents and concentration gradients in multi-ion systems with its relation to the microenvironment at the electrode (such as pH^{25,26}) display an important design aspect for electrochemical devices for batteries^{21–23}, the separation of ions^{27,28}, CO_2 reduction^{29,30}, electrowinning^{31,32}, electroplating^{33–35} and so forth.

In binary electrolytic solutions, the electrolyte parameterization is described by the transfer numbers (that describe the different contributions of the anions and cations to the conduction), the mutual diffusion coefficient (pairwise diffusion of anions and cations under the boundary condition of electro-neutrality in the solution) and the molar conductivity. These properties depend on the concentration,

for which the electrochemically driven concentration gradients require a spatially resolved parameterization for a precise transport modeling ²⁴. Numerical time domain modeling of the electrochemical transport differential equations has proven its reliability to represent the concentration dependence of the electrolyte parameterization, while it also can resolve changing boundary conditions such as varying currents ²⁴.

The ion transport with supporting electrolytes was modeled in previous studies with analytical ^{36–38} and numerical ^{39–41} approaches to solve the electrochemical transport equations. From these studies, only Awakura et al. ³⁷ compared model results with experimental data, which is however crucial to understand and describe the complexity of the ion-ion interactions in these systems that cannot be precisely described by ab-initio models. All of these studies were conducted with a constant set of electrolyte parameters that do not take into account the concentration dependence and ion-ion interactions. Most of these studies considered an infinite distance of anode and cathode ^{37–39,41}, which simplifies the mathematical description and analytical solution of the transport equations. This scenario however does not lead to a steady state with a constant limited current ²⁴. A detailed understanding of the mechanisms that influence limited current in supported electrolytes, its correlation to the electrolyte properties and the parameterization of the interaction of different sort of ions is not yet reported.

The aim of this study is to describe the ion transport in supporting electrolytes with a physical time domain model of the electrochemical transport equations which enables a concentration-dependent parameterization and the description of steady limited currents. The modeled limited currents are compared under different parameterization scenarios to measured limited currents of mixed CuSO_4 and Na_2SO_4 electrolytes. To understand the physicochemical mechanisms of the ion transport in supported electrolytes and its influence on the limited current in detail, a computationally sensibility analysis of the parameterization is conducted. Moreover, the computer model is adjusted to multi-ion systems in molten salts and ionic liquids, showing similarities and differences of the ion transport in comparison to the solvent-based electrolytes. The source codes of the computational model are provided in the supporting information, so that the community effortlessly can reproduce the presented results and thereon further develop the presented model.

2 Methods

2.1 Experimental

In this study, the copper deposition and dissolution of plane and polished copper electrodes in mixed CuSO_4 and Na_2SO_4 electrolytes serve as an exemplary system to examine limited currents. Hereto, the two polished copper plates are separated by a stamped fluoroelastomer flat sealing with an inner diameter of 14 mm and a thickness of 500 μm (Reichelt Chemietechnik). To assemble the cell, the sealing was laid on one electrode and the copper surface was wetted with approximately 1 ml of electrolyte. The surface of the other electrode was also wetted with the electrolyte and then pressed onto the electrode with the sealing. Thereby, the excess electrolyte floated out of the cell assembly while the sealing between the electrodes was completely filled with the electrolyte. The anode was placed at the bottom to avoid macroscopic density differences that are compensated by gravitational shear forces ²⁴. An additional cell with copper electrodes and an electrode distance of 20 mm was used to characterize the conductivity of Na_2SO_4 solutions. Hereto, the copper electrodes were pressed with flat sealings (same type as above) on a polypropylene body. With 4-wire potentiodynamic alternating current impedance measurements, the electrolyte resistance was determined ⁴².

2.2 Model

A detailed model on the ion transport in binary electrolytes has been presented previously²⁴, which included an experimental evaluation and a concentration-dependent parameterization of the conductivity, mutual diffusion coefficient and ion transfer number. This transport model describes the electric field and diffusion driven motion of dissolved ions in liquid electrolytes and is in the following adapted to an electrolyte with three ion types. The aim is here to parameterize the multi-ion system on the basis of reported experimental conductivities, diffusion coefficients and transfer numbers on the binary electrolyte systems of CuSO_4 and Na_2SO_4 , respectively. The source codes of this approach are supplied in the supporting information.

Figure 1 summarizes the data on molar conductivity, diffusion coefficient and cation transfer number of aqueous CuSO_4 and Na_2SO_4 electrolyte solutions, respectively, referring to the data reported by Owen et. al⁴³, Bester-Roag et. al⁴⁴, Emanuel et. al⁴⁵, Noulty et. al⁴⁶, Woolf et. al⁴⁷, Rard et. al⁴⁸, Pikal et. al⁴⁹ and Longworth et. al⁵⁰. The molar conductivity and diffusion coefficients decrease towards higher electrolyte concentrations, which is a direct result of the ion-ion interaction that is described by the Debye-Hückel theory^{51,52}. Most of the literature reported values at the standard temperature of 25°C, whereas the measurements in this study were performed at 20°C. The effect of temperature on the molar conductivity and diffusion coefficient is treated as discussed elsewhere in detail²⁴. The conductivity and the transfer coefficient of the CuSO_4 electrolyte show a more distinct concentration dependence than those of the Na_2SO_4 electrolyte. The dissolution of CuSO_4 acidifies the aqueous solvent, however, the concentration of protons is more than 1000 smaller than the concentration of dissolved copper for which the impact on protons on the transport model is negligible²⁴. The trends of the concentration dependence of the electrolyte properties can be described on the basis of the Debye-Hückel theory, whereas the complexity of the aqueous solutions do not allow a precise theoretical prediction of ion-ion interactions and their impact on conductivities and diffusion coefficients^{53,54}. Thus, the experimental data is described by analytical non-physical equations which adequately describe the concentration dependence of the literature data in Figure 1 as discussed in the supporting information in detail.

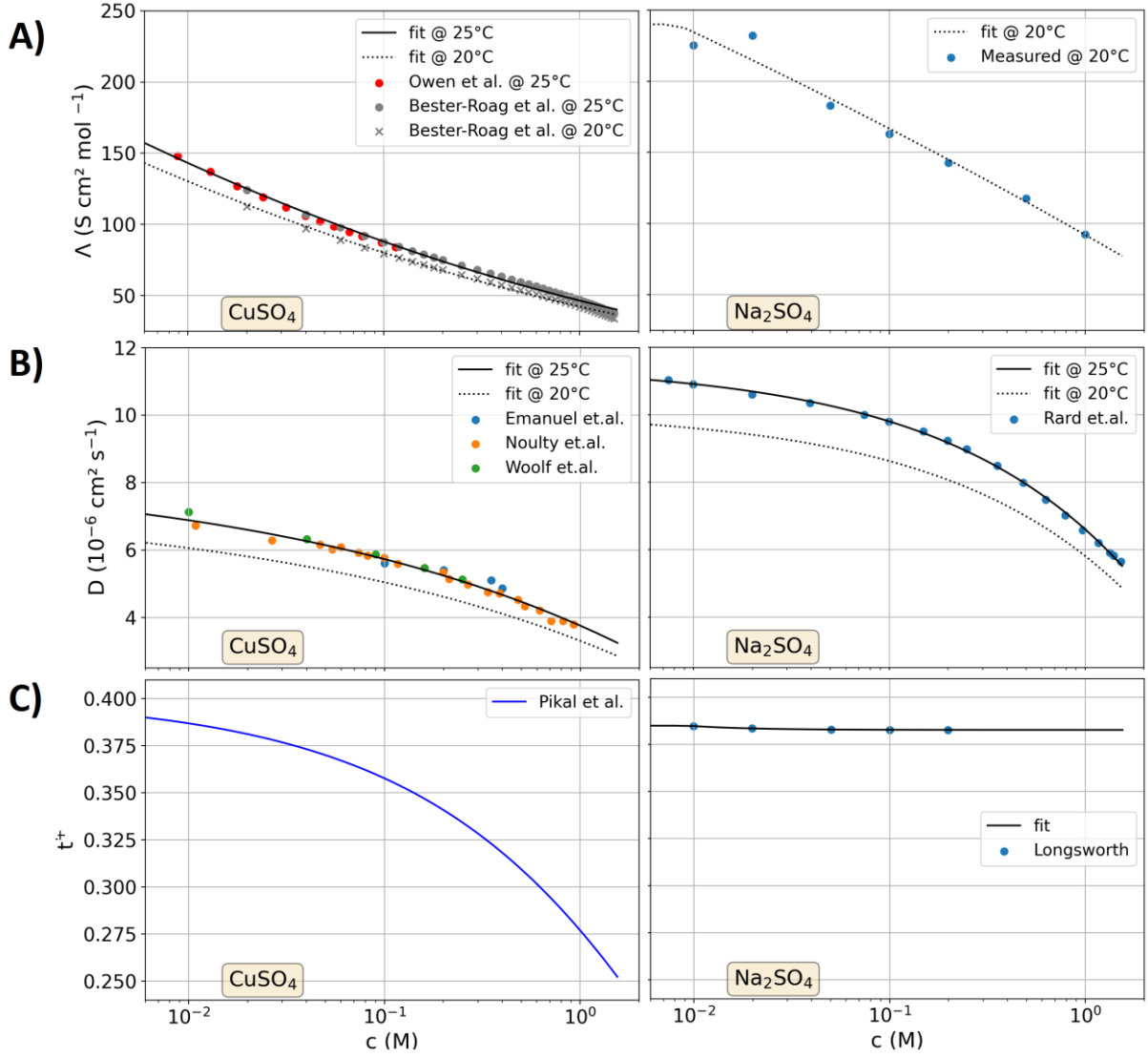


Figure 1: Parameterization of CuSO_4 (left) and Na_2SO_4 (right) binary electrolytes as a function of the concentration. A) Molar conductivity. B) Diffusion coefficient. C) Transfer number.

The transfer number t^i of the ion type i is defined by the current I^i that it carries in relation to the total current I_{tot} :

$$t^i = \frac{I^i}{I_{\text{tot}}} \quad (1)$$

Using Ohm's law, this equation can also be interpreted as a ratio of conductivities κ :

$$t^i = \frac{\kappa^i}{\kappa_{\text{tot}}} \quad (2)$$

To apply this definition to multi-ion systems, a more precise notation is introduced in the following. In Na_2SO_4 , the anion (SO_4^{2-}) has a valence of two whereas the cation (Na^+) has a valence of one. By using the lowest common denominator of the valences, equal charges and equal concentrations of the definitions of $C = 2\text{Na}^+$ and $A = \text{SO}_4^{2-}$ result. The molar conductivity Λ of an binary electrolyte that is comprised by type A and C is here defined as Λ^{AC} (units of $\text{S cm}^2 \text{ mol}^{-1}$). As shown in Figure 1, the transfer number and the molar conductivity have an intrinsic concentration dependence for which

both are a function of the concentration c^{AC} . The conductivity of the binary electrolyte κ^{AC} equals the product of concentration and molar conductivity:

$$\kappa^{AC} = c^{AC} \times \Lambda^{AC} \quad (3)$$

With the molar conductivity and the ion transport number, the conductivity κ^A of the anion A as a function of the concentration can be calculated as

$$\kappa^A = c^{AC} \times t^A \times \Lambda^{AC} \quad (4)$$

In the considered multi-ion system of CuSO_4 with Na_2SO_4 addition, the conductivity of the sodium and copper ions are determined similarly to the binary solutions

$$\kappa^{\text{Cu}^{2+}} = t^{\text{Cu}^{2+}} c^{\text{CuSO}_4} \hat{\Lambda}^{\text{CuSO}_4} \quad (5)$$

$$\kappa^{2\text{Na}^+} = t^{2\text{Na}^+} c^{\text{Na}_2\text{SO}_4} \hat{\Lambda}^{\text{Na}_2\text{SO}_4} \quad (6)$$

where $\hat{\Lambda}$ includes the influence by the interactions between the different ion types on the molar conductivity. In the case of the sulfate anion, the situation becomes more complex, as it is involved in the conduction of both salts. Its conductivity is here calculated as the sum of its contributions to the conductivity of both dissolved salts:

$$\kappa^{\text{SO}_4^{2-}} = [1 - t^{\text{Cu}^{2+}}] c^{\text{CuSO}_4} \hat{\Lambda}^{\text{CuSO}_4} + [1 - t^{2\text{Na}^+}] c^{\text{Na}_2\text{SO}_4} \hat{\Lambda}^{\text{Na}_2\text{SO}_4} \quad (7)$$

In the results part, different approaches to estimate the influence of the ion interactions on the molar conductivity are presented, which are based on previously reported data on the binary electrolytes. The total conductivity κ_{tot} in the multi-ion system equals the sum of the conductivities of the individual types of ions discussed above. Accordingly, the conductivity ratio (equation 2) can be determined for multi-ion systems, which expressed the share of the different ion types to the overall current and thus determines the conductivity-driven ion motion in the ion transport model.

The diffusion process of type A and C is always pairwise, as otherwise the electroneutrality is violated. Thus, the mutual diffusion coefficients D are used to calculate those of the cations:

$$D^{\text{Cu}^{2+}} = D^{\text{CuSO}_4} \quad (8)$$

$$D^{2\text{Na}^+} = D^{\text{Na}_2\text{SO}_4} \quad (9)$$

For the sulfate ions, the weighted arithmetic mean is used to calculate the diffusion coefficient, as their diffusion also depends on the mobility of the cations to which they are paired:

$$D^{\text{SO}_4^{2-}} = \frac{c^{\text{CuSO}_4} D^{\text{CuSO}_4} + c^{\text{Na}_2\text{SO}_4} D^{\text{Na}_2\text{SO}_4}}{c^{\text{CuSO}_4} + c^{\text{Na}_2\text{SO}_4}} \quad (10)$$

The differential equations of the transport model is discussed in the supporting information in detail, including their boundary conditions at the electrodes and their implementation in the numerical simulation framework.

3 Results and discussion

First, the experimental and model data on the ionic transport of mixed CuSO_4 and Na_2SO_4 electrolytes is presented. Second, the influence of the electrolyte parameters on limited currents is examined using the transport model. Moreover, the computer model is used to describe the transition from diluted polar solvents to ionic liquids, highlighting similarities and differences of both systems.

3.1 Measured and modeled data on the CuSO_4 - Na_2SO_4 electrolytes

Figure 2 shows the measured current densities of a 0.1 M CuSO_4 solution with a variation of Na_2SO_4 addition from 0 to 1 M as a function of time. A voltage of 0.3 V was applied between the electrodes that were 500 μm apart from each other and separated by a polymer sealing (see experimental section). After initial double layer charging and surface reduction/oxidation the current can be mainly attributed to the copper deposition and dissolution. This electrochemical current decays over time as the cathodic copper ion concentration depletes (detailed discussion below). After approximately 200 seconds a steady current is reached for all different concentrations.

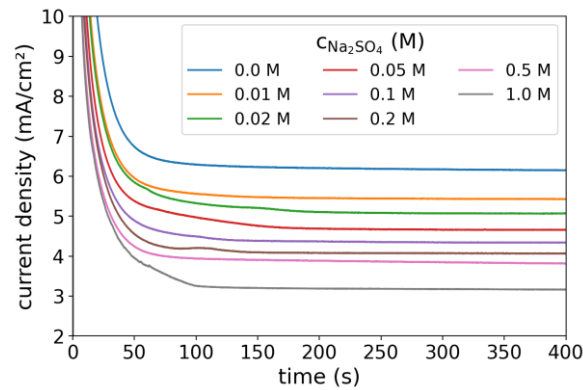


Figure 2: Measured current densities at 0.3 V between two copper electrodes with a CuSO_4 concentration of 0.1 M and a variation of the Na_2SO_4 concentration from 0 to 1 M.

To calculate the limited currents with the transport model, the simulation is started with a current density of 15 mA/cm^2 that is larger than the expected limited currents, resembling the experimental approach. When the concentration of copper ions at the cathode depletes to 1/15 of the initial concentration of 0.1 M, the current is decreased. After this initial reduction, the current is continuously adjusted so that the cathodic copper ion concentration is ranging between 1/15 and 1/12 of the initial concentration. Figure 3 shows an example of the modeled concentration gradients between the electrodes for a total CuSO_4 concentration of 0.1 M and a Na_2SO_4 concentration of 0.2 M. In the initial state, the concentration of the ions is evenly distributed in the electrolytic solution. In the final state, a steady limited current is reached, in which the concentration gradients do not change as a function of time and in which the copper ion concentration at the cathode is depleted. The total concentrations of the ions in the electrolyte do not change, as the inert ions are not converted at the electrodes and as the same amount of copper is deposited and dissolved. Moreover, the sum of the charges of the cations and anions is locally and globally zero, fulfilling the framework of electroneutrality of the electrolyte (see detailed discussion in reference ²⁴).

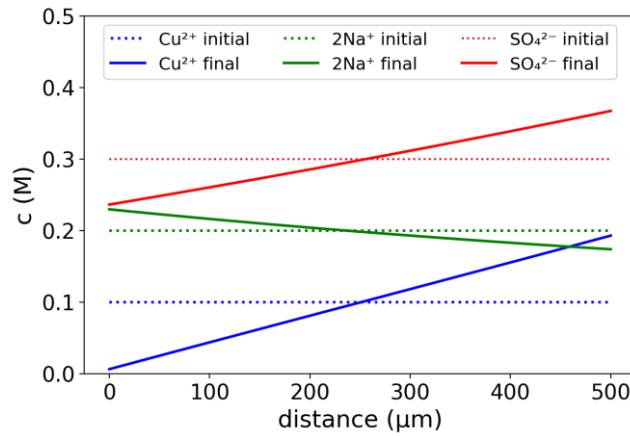


Figure 3: Modeled concentration gradients (using the parameterization case iv as defined in the text below) of the limited current for an electrode distance of 500 μm , a CuSO_4 concentration of 0.1 M, and a Na_2SO_4 concentration of 0.2 M. The cathode is located at the left side (distance = 0) and the anode at the right side (distance = 500 μm).

In contrast to the copper ion starvation at the cathode and its accumulation at the anode, the sodium ion concentration gradient is converse, with an enlarged amount at the cathode and a reduced amount at the anode. The sodium ions are transported by the electric field in the electrolyte to the cathode where they cannot be converted. In the steady state, the sodium ion current by the electric field is balanced by diffusion into the opposite transition, leading to no net sodium ion transport. As the sulfate ions are transported by the electric field towards the anode, the amount of sulfate ions is decreased at the cathode and increased at the anode. As the sulfate ions are the only anions in this system, their amount reflects the total amount of dissolved ions with respect to the charge. Similar to the sodium ions, in the steady state the net sulfate ion transport equals zero so that the copper ions as the only electrochemical active ion type constitute the net current. The electric-field and diffusion-driven ion transport of the copper ions point in the same direction from the anode to the cathode.

From the measurements graphed in Figure 2, the limited current was determined by the mean current between 300 and 400 seconds after the experiments started. In addition to the data graphed in Figure 2, two repetitions were made. Figure 4 shows the mean of these measurements with the standard variation as the statistic error of the experiments. Moreover, Figure 4 shows the modeled data, which is considered for four different approaches of the parameterization, which all show similar trends to the experiment with decreasing limited currents towards higher Na_2SO_4 concentrations. The four different parameterizations are characterized by the following features:

(i) The first case is modeled with a constant parameterization, resembling previously reported models in the literature^{36–41}. The values of Figure 1 at 0.1 M concentration of CuSO_4 and Na_2SO_4 serve as model input parameters. When the concentration of copper ions near the cathode is thinning out, their local conductivity, diffusion coefficient and transfer number increase with reference to Figure 1 which increases the limited current in pure CuSO_4 electrolytes²⁴. By neglecting these concentration dependencies, the current is up to a Na_2SO_4 concentration of 0.5 M underestimated (similar to that in binary solutions²⁴), as the locally higher diffusivity and ion transport number (see Figure 1) of the copper ions at the depleting cathodic concentration is not taken into account. At higher Na_2SO_4 concentrations, the decrease of the conductivity, diffusion coefficients and transfer number becomes significant so that the model with the constant parameterization overestimates the limited current.

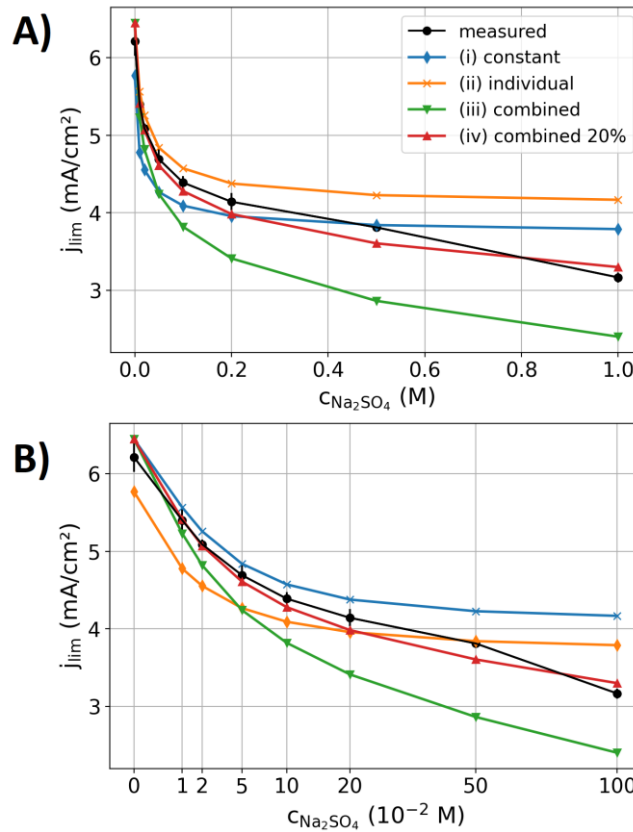


Figure 4: Measured (black lines with scatter and error bars) and modeled (colored lines) limited currents for a CuSO₄ concentration of 0.1 M under a variation of the Na₂SO₄ concentration. The four different parameterization scenarios for the model are discussed in the text. The measured data is recorded with a voltage of 0.3 V between the electrodes. A) Linear increment of the x-axis. B) Square root spacing of the x-axis to more clearly resolve the small concentrations.

(ii) In the second case, the model is parameterized with the individual concentration dependencies of CuSO₄ and Na₂SO₄ respectively, without taking their interaction into account. Thus, the molar conductivity, diffusivity and cation transport number of the CuSO₄ component decreases towards higher CuSO₄ concentrations, whereas it is not affected by the Na₂SO₄ concentration. Likewise, the properties of the Na₂SO₄ component are influenced by its concentration and does not interact with the CuSO₄ component. The modeled data is overestimating the measured limited current. At Na₂SO₄ concentrations below 0.05 M the differences between the modeled and measured data is with less than 5 % moderate, however, it increases towards higher concentrations. As expected from the Debye-Hückel theory, the interaction of the ions is expected to decrease the molar conductivity and diffusion coefficients, explaining the modeled overestimation of the limited currents.

(iii) In the third parametrization scenario, the parameters of the CuSO₄ and Na₂SO₄ components are calculated as a function of the total concentration of sulfate ions, assuming that the interaction between the sulfate ions and the cations is equal. However, this parametrization underestimates the measured limited current. Thus, the assumption that the ions influence one another in the same amount does not hold valid. Figure 1 showed a more pronounced concentration dependence of molar conductivity, diffusion coefficient and transfer number of CuSO₄ than that of Na₂SO₄. Thus, the ion-ion interactions in CuSO₄ are different from that in Na₂SO₄ and the influence of the different components on one another is therefore also not that easy to describe.

(iv) The fourth case stands for a concentration-dependent parameterization that displays a mixture between the second and third approach. Hereto, the parameters for the CuSO₄ component are

calculated for the concentration of CuSO_4 plus 20% of the concentration of Na_2SO_4 . Analogously, the parameters for the Na_2SO_4 component are calculated for the concentration of Na_2SO_4 plus 20% of the concentration of CuSO_4 . Thus, an interaction between the different ion types is partly included, however, to a smaller extent than that between the ions of the same type. Using this parameterization, a good fit of modeled and measured data is obtained.

The scenarios discussed above are based on the experimental data on binary electrolytes and do not represent a physicochemical approach to characterize the ion-ion interactions in mixed ion systems. Based on these data, however, the ion-ion interaction is shown to crucially impact the ion transport in supporting electrolytes and the related limited currents. In the literature⁵³, the Debye-Hückel theory based physicochemical models that are used to describe the complex interaction between the ions are non-trivial and typically do not exactly describe the concentration dependence of the electrolyte parameters. However, using such approaches a physicochemical description of the ion-ion interactions for the electrolyte parameterization may be possible. Theoretical works to address the prediction of the ion-ion interaction in multi-ion systems have to follow and may lead to more precise parameterization procedures as the presented approaches that is based on the experimental data of binary electrolytic solutions.

3.2 Computational Sensibility Analysis

Thus far, measured and modeled data showed that limited currents decrease towards higher concentrations of the inert ions. The aim of the following section is to consider the modeled limited currents under a variation of the electrolyte parameters, aiming to display the physicochemical relations that are described by the differential equations of the transport model. Hereto, two cases are considered, a polar solvent in which the salts are dissolved and an ionic liquid (or ionic melt). The first case resembles the above discussed CuSO_4 - Na_2SO_4 system, where water displayed the polar solvent.

A simplified test system is considered in the following, in order to focus on the physicochemical interactions of the transport mechanisms rather than the complex parameterization that is discussed above. The test system is characterized by the following properties: 1) The electrolyte is comprised by two different salts, with two different types of cations (denoted as C1 and C2) and one type of anion (denoted as A). 2) Cation type C1 is pushed at the anode into the electrolyte and it is removed at the cathode, the other ions are inert. 3) Both salts have an equal density. 4) The molar conductivity, diffusion coefficient and transfer number of both salts are assumed as concentration independent with constant values of $\Lambda = 100 \text{ S cm}^2 \text{ mol}^{-1}$, $D = 10^{-5} \text{ cm}^2 \text{ s}^{-1}$, $t^+ = 0.5$ and initial concentrations of $c = 0.1 \text{ M}$. One of these parameters of the supporting salt (C2 and A) are varied, while the other remain constant.

Figure 3 showed, that the net concentration of all ions at the cathode in the system decreases near the cathode. However, in the case of ionic liquids or salt melts, the depletion of the ions at an electrode means that the entire electrolyte vanishes whereas it concentrates at another electrode. For the test system with the ionic liquid an encapsulated volume is considered (such as in a battery). As both salts in the test system have the same type of anions and the same density, only the positions of the cations can change whereas the concentration of the anions is constant over the entire electrolyte. Hence, the differential equations that describe the anion transport are neglected and deleted from the source code.

Figure 5A shows the modeled concentration gradients of the test system with a polar solvent. Despite the different parameterization, a similar shape of the concentration gradients compared to Figure 3 is obtained. Figure 5B graphs the limited currents that are obtained under the parameter variation of the electrolyte with the polar solvent. With a negligible concentration or conductivity of the inert cations

C2, the same limited current as in the case of the unsupported electrolyte is reached. With an increasing concentration or conductivity the limited current drops to the value described by Fick's first law, in which diffusion is the only driving force. Thus, in this case the conduction of C1 has a minor impact on its net transport. Without the supporting salt, the limited current is approximately 2 times higher than that described by Fick's first law. In the case of a variation factor of unity (equal properties of inert and active salt), the limited current is 1.25 higher than the diffusion-limited current.

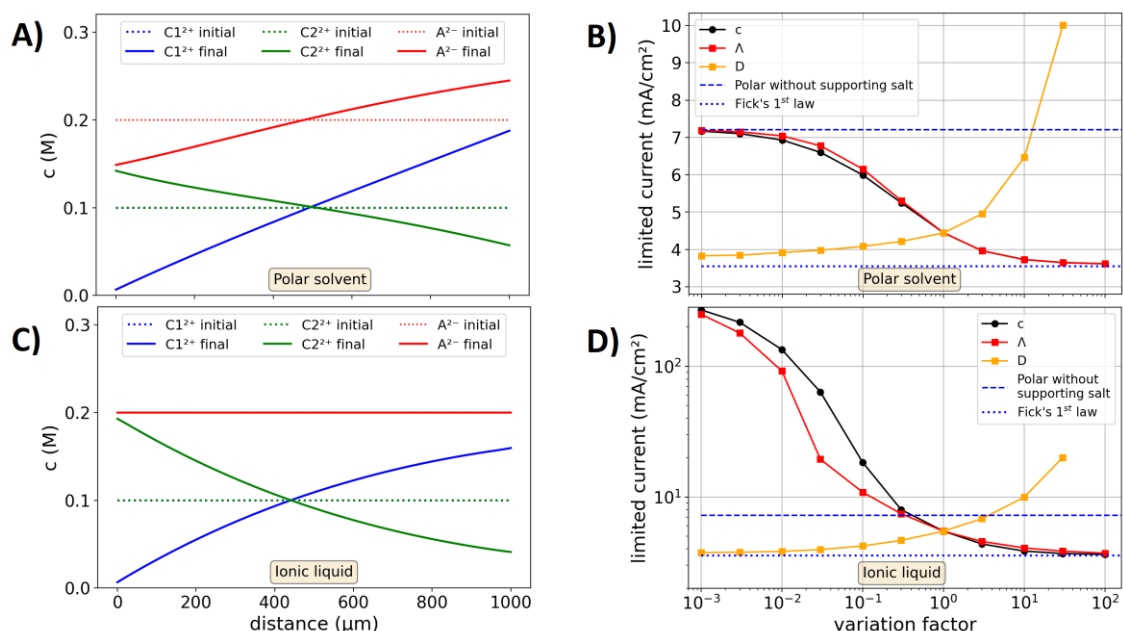


Figure 5: Modeled data to examine the influence of the electrolyte parameters on the limited current for an electrode distance of 0.1 cm , an initial concentration of $c = 0.1 \text{ M}$, a molar conductivity $\Lambda = 100 \text{ S cm}^2 \text{ mol}^{-1}$ and a diffusion coefficient of $D = 10^{-6} \text{ cm}^2 \text{ s}^{-1}$ of the supporting salt and the reactive ion pair. A) Concentration gradients obtained for the polar solvent. B) Parameter variation for the polar solvent. The variation factor on the x-axis is multiplied to one of the properties of the supporting salt. Blue lines: Diffusion-limited current calculated by Fick's first law and the limited current without addition of supporting salt. C and D) Same as (A) and (B) but for an ionic liquid, where the ion displacement is confined as described in the text in more detail.

In binary diluted electrolytes (polar solvent) the conductivity does not influence the limited current, as the entire current is anyway carried by the ions²⁴. However, as here defined by the conductivity ratio, now the conductivity is decisive as it determines how much of the active ions C1 are actually carried by the conduction. The conductivity is shared between the different types of ions. When the conductivity of the inert ion C2 type becomes much larger than that of the active ion C1, the ion C1 is mainly transported by the driving force of the concentration gradient as the conduction is mainly done by C2. The limited current increases towards higher values of the diffusion coefficient of the inert salt. In this case, a depletion of ions at the cathode is avoided, from which also the limited current benefits.

Figure 5C shows the concentration gradient modeled for an ionic liquid. In this case, the amount of anions is constant over the distance (see discussion above). Figure 5D shows the modeled limited currents for the ionic liquid scenario. Without the supporting salt, the limited current is infinite as the boundary condition of the constant anion concentration does not allow a concentration gradient. With small additions of the supporting electrolyte, the supporting salt accumulates at the cathode and high concentration gradients of C1 over small distance close to the cathode result, for which the limited currents are orders of magnitude higher than those in the case of the polar solvent. Towards infinite

concentrations or conductivities of C2, the limited current drops to the diffusion-limited current described by Fick's first law (see reference ²⁴).

3.3 Application of the Results in Electrochemical Devices

The results on the copper based model system can find direct application in the design of electrochemical processes and devices such as copper refining^{4,5} or aqueous copper/sulfur batteries^{55,56}. However, the aim of this article is to conclude physicochemical relations that are applicable to a wider scope which are independent of the parameterization of the presented model system that may help in the design of electrochemical applications. With knowledge that the limited current decreases with the amount of supporting ions, the addition of inert ions displays a compromise between an increased conductivity and a decreased limited current. When the electrolyte is mechanically mixed by convectional forces, the concentration gradients formed by the electrochemical current are partly equilibrated. Thus, the diffusion-limited currents increase in comparison to the case of static electrolytes. Causes for such convection can be found in: (i) Macroscopic density difference, where the gravitational force leads to shear forces. (ii) Bubble formation and ascending bubbles. (iii) Mechanical mixing of the electrolyte by stirring or pumping.

In ionic liquids, the electrode is always in contact with the electrolyte, which reduces with reference to Figure 5 the depletion of the active ion type at the electrode in comparison to solvent based electrolytes. However, high viscosities typically cause smaller diffusion coefficients and conductivities of the active ion types in ionic liquids than that those of solvent based electrolytes. As a result, limited currents can display a severe limitation for electrochemical devices and processes that operate with ionic liquids.

4 Conclusion

This study examined the ion conduction, current-driven concentration gradients and related limited current in supporting electrolytes. A computational model is developed to characterize the ion transport and the related spatiotemporal ion concentrations in supporting electrolytes. This model is equipped with different concentration-dependent parameterization scenarios and evaluated with measured limited currents of CuSO₄ - Na₂SO₄ supporting electrolytes. The comparison of measured and modeled data shows that a complex concentration-dependent parameterization of the interaction between the different ion types in the supporting electrolyte is required to adequately model the ion transport. A computational study on the variation of the electrolyte parameters reveals the ion transport mechanisms and the interplay of electric-field and diffusion-driven ion motion. With an infinite amount of supporting salt in the electrolyte, the conduction-driven transport of the active ion becomes negligible and the limited current drops to the diffusion-limited current that is described by Fick's first law. By changing the framework of the developed model, the transition from supporting electrolytes to ionic liquids (and ionic melts) is examined, revealing similarities and differences of the transport mechanisms and their impact on limited currents.

5 Data availability

All data of the computational model generated or analysed during this study are included in this published article and its supporting information as it can be calculated and reproduced with the provided source code. The experimental datasets used and/or analysed during the current study are available from the corresponding author on reasonable request

6 Supporting Information

The supporting information contains:

- Differential equations of the ion transport model
- Fit equations and parameters for the concentration dependence of the electrolyte properties
- Computer code (programming language Python) of the ion transport model

7 Acknowledgement

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